

CS 476 – Programming Language Design

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Questions

Nobody has responded yet.

Hang tight! Responses are coming in.

Structure of a Language

➤ Syntax

- Abstract – what are the pieces of a program?
- Concrete – what do programs look like?

• Semantics

- Static – what are acceptable programs?
- Dynamic – what do programs do when we run them?

• Pragmatics

- Implementation – how can we actually make the semantics happen?
- IDE, tool support, etc.

Metalanguages

- We want to describe how languages should work, and write code that actually runs those languages
- Natural language: “ $x := y + z$ sets x to be y plus z ”
- Inference rules:
$$\frac{(e, \sigma) \Downarrow v}{(x := e, \sigma) \Downarrow \sigma[x \mapsto v]}$$
- OCaml: `match s with
| Assign x e => update env x (eval env e)`
- We'll learn to *translate* between these three metalanguages!

Defining Syntax for a Language

- This language has *expressions* and *commands*
- *Expressions* are things like adding or subtracting two numbers, or calling a function
- *Commands* include assigning values to variables, and if-then-else blocks

Defining Syntax for a Language

- This language has *expressions* E and *commands* C
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Defining Syntax for a Language

- This language has *expressions* E and *commands* C
- $E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$
- *Commands* include assigning values to variables, and if-then-else blocks

Defining Syntax for a Language

- This language has *expressions* E and *commands* C
- $E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$
- $C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \}$

Context-Free Grammars

- A series of rules describing a set of strings (“language”)
- Each rule has a *nonterminal* on the left, and a sequence of *nonterminals* and *terminals* (letters, numbers, operators, etc.) on the right

$E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$

$C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \}$

nonterminals: $E C$ terminals: $\langle \text{num} \rangle \langle \text{name} \rangle + () = ; \text{if else} \{ \}$

Context-Free Grammars

- A series of rules describing a set of strings (“language”)
- Any string that can be made by applying the rules belongs to the language

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C

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$C \Rightarrow x = E ;$

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$C \Rightarrow x = E ; \Rightarrow x = f (E) ;$

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$C \Rightarrow x = E ; \Rightarrow x = f (E) ; \Rightarrow x = f (2 + 4) ;$

A program in the language of the grammar

- This is “just syntax”: it doesn’t do anything yet!

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Context-Free Grammars

- A series of rules describing a set of strings (“language”)
- ...that looks a lot like an inductive datatype!

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$C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \}$

type E = Add | Call

type C = Assign | If

Context-Free Grammars

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- We’re interested in the *abstract* syntax, the parts that can vary

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type E = Add of int * int | Call

type C = Assign | If

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type E = Add of int * int | Call of name * E

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type E = Add of int * int | Call of name * E

type C = Assign of name * E | If of E * C * C

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Grammars: Variations

$E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$

$C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \}$

type E = Add of int * int | Call of name * E

type C = Assign of name * E | If of E * C * C

- Exercise: Change one thing about the grammar of the language. How would that change the OCaml types?

Grammars: Variations

$E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$

$C := \langle \text{name} \rangle := E \mid \text{if } E \text{ then } C \text{ else } C$

type E = Add of int * int | Call of name * E

type C = Assign of name * E | If of E * C * C

- Exercise: Change one thing about the grammar of the language. How would that change the OCaml types?

Grammars: Variations

$E := \langle \text{num} \rangle + \langle \text{num} \rangle - \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$

$C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \}$

type E = Add of int * int * int | Call of name
* E

type C = Assign of name * E | If of E * C * C

- Exercise: Change one thing about the grammar of the language. How would that change the OCaml types?

Grammars: Variations

$E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E) \mid \langle \text{num} \rangle * 2$

$C := \langle \text{name} \rangle = E ; \mid \text{if} (E) \{ C \} \text{else} \{ C \} \mid C ; C$

```
type E = Add of int * int | Call of name * E |  
Mul2 of int
```

```
type C = Assign of name * E | If of E * C * C |  
Seq of C * C
```

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Grammars: Variations

$E := \langle \text{num} \rangle + \langle \text{num} \rangle \mid \langle \text{name} \rangle (E)$

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Defining Syntax for a Language

- Step 1: write down what's in the language in English
- Step 2: write a grammar that describes all possible programs
- Step 3: write a datatype that abstracts the grammar
- Result: a datatype of *programs in the language*

Writing Functions on Syntax

```
type E = Add of int * int | Call of name * E
```

```
type C = Assign of name * E | If of E * C * C
```

```
let my_prog : C = If (Add (3, 4), Assign ("x", Add (3, 4)), ...)
```

```
let rec print_vars (prog : C) =  
  match prog with  
  | Assign (x, e) -> print_string x  
  | If (cond, tcase, fcase) ->  
    print_vars tcase; print_vars fcase
```

Writing Functions on Syntax

- Step 1: write down what's in the language in English
- Step 2: write a grammar that describes all possible programs
- Step 3: write a datatype that abstracts the grammar
- Result: a datatype of *programs in the language*

- Now we can write programs that operate on programs!

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