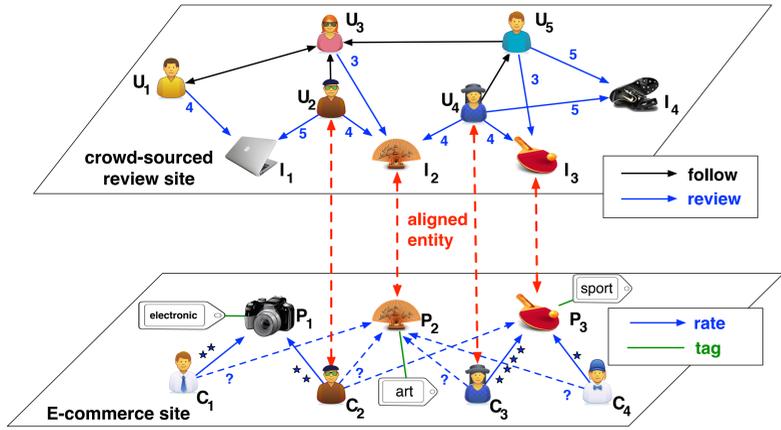


1. Item Recommendation for Emerging Businesses



- (I) Emerging Business: new network with very sparse information.
- (II) Partially Aligned Networks: networks sharing common entities

- * How to measure similarity between users/items with sparse information?
- * How to utilize information from aligned networks to improve performance?

Hint: Transfer knowledge through aligned entities.

3. Recommendation Model: AmpCMF

$$\min_{\mathbf{P}^{(\pi)}, \mathbf{Q}^{(\pi)} \geq 0, \pi \in \{s, t\}} \mathcal{J} = \sum_{\pi \in \{s, t\}} \|\mathbf{I}^{(\pi)} \odot (\mathbf{Y}^{(\pi)} - \mathbf{P}^{(\pi)} \mathbf{Q}^{(\pi)T})\|_F^2 + \beta (\mathcal{R}_A(\mathbf{P}^{(t)}, \mathbf{P}^{(s)}) + \mathcal{R}_A(\mathbf{Q}^{(t)}, \mathbf{Q}^{(s)})) + \lambda (\mathcal{R}_G(\mathbf{P}^{(t)}) + \mathcal{R}_G(\mathbf{Q}^{(t)})) + \frac{\alpha}{2} \sum_{\pi \in \{s, t\}} (\|\mathbf{P}^{(\pi)}\|_F^2 + \|\mathbf{Q}^{(\pi)}\|_F^2)$$

Collective Matrix Factorization (CMF) w/ alignment regularization

geometric regularization

prevent overfitting

\mathbf{Y} and $\mathbf{I} \in \mathbb{R}^{n \times m}$ are user-item feedback and indicator matrices

$\mathbf{P} \in \mathbb{R}^{n \times k}$ and $\mathbf{Q} \in \mathbb{R}^{m \times k}$ are low rank representations of users and items

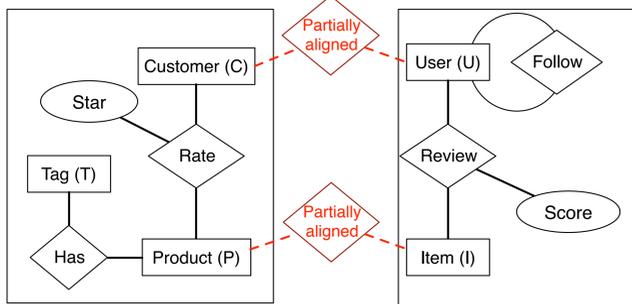
alignment regularization: $\mathcal{R}_A(\mathbf{P}^{(t)}, \mathbf{P}^{(s)}) = \frac{1}{2} \sum_{(i, g_i) \in \mathcal{A}(t, s)} \|\mathbf{p}_i^{(t)} - \mathbf{p}_{g_i}^{(s)}\|_2^2 = \frac{1}{2} \|\mathbf{A} \mathbf{A}^T \mathbf{P}^{(t)} - \mathbf{A} \mathbf{P}^{(s)}\|_F^2$

geometric regularization: $\mathcal{R}_G(\mathbf{P}) = \frac{1}{2} \sum_{u, v} \mathbf{S}_{uv} \|\mathbf{p}_u - \mathbf{p}_v\|_2^2 = \frac{1}{2} \text{Tr}(\mathbf{P}^T (\mathbf{D} - \mathbf{S}) \mathbf{P}) = \frac{1}{2} \text{Tr}(\mathbf{P}^T \mathbf{L}_P \mathbf{P})$

◆ Solve the optimization problem using multiplicative updates

2. Augmented Meta Path-based Similarity (AmpSim)

Schema of partially aligned networks



Examples of Augmented Meta Path (AMP)

Intra-network augmented meta path

$$(C \xrightarrow{[star]} P \xrightarrow{[star]} C), (P \xrightarrow{[star]} C \xrightarrow{[star]} P), (P \rightarrow T \leftarrow P)$$

$$(C \xrightarrow{[star]} P \xrightarrow{[star]} C \xrightarrow{[star]} P \xrightarrow{[star]} C)$$

$$(P \xrightarrow{[star]} C \xrightarrow{[star]} P \xrightarrow{[star]} C \xrightarrow{[star]} P)$$

both linkage structures and augmented link attributes are taken into account

Inter-network augmented meta path

$$(P \leftrightarrow I \xrightarrow{[score]} U \xrightarrow{[score]} I \leftrightarrow P)$$

$$(C \leftrightarrow U \xrightarrow{[score]} I \xrightarrow{[score]} U \leftrightarrow C), (C \leftrightarrow U \leftrightarrow U \leftrightarrow C)$$

How to measure similarity via AMPs?

Normalize link attributes to deal with different types of link attributes upon an AMP:

$$\mathbf{M}_{ui} = \frac{Y_{ui} - b_i}{\sqrt{\sum_j (Y_{uj} - b_j)^2}}$$

\mathbf{Y} : link attributes
Ordinal attributes: $b_i = \bar{Y}_i$
Other attributes: $b_i = 0$

After normalization, $\mathbf{M} \mathbf{M}^T$ is (adjusted) cosine similarity

AmpSim: AMP-based similarity measure between v_a and v_b based on path \mathcal{P}

$$s(v_a, v_b | \mathcal{P}) = \frac{\prod_{i=1}^l \mathbf{M}_i |_{ab} + \prod_{i=1}^l \mathbf{M}_i^T |_{ba}}{\prod_{i=1}^l \mathbf{M}_i |_{a*} + \prod_{i=1}^l \mathbf{M}_i^T |_{b*}} \in [0, 1]$$

path direction is taken into account

$\prod_{i=1}^l \mathbf{M}_i$ is the product of the normalized link attributes upon \mathcal{P}

Average over multiple AMPs:

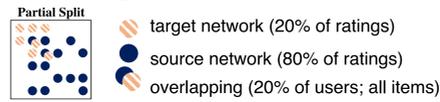
$$S(v_a, v_b) = \frac{\tanh(\sum_i w_i S_i(v_a, v_b))}{\tanh(1)} \in [0, 1] \quad \sum_i w_i = 1$$

4. Experiment Results

Name	#users	#items	#tags	#ratings	#social links
Yelp	26,618	8,467	770	230,418	183,765
Epinions	21,740	31,678	27	541,108	344,286

Yelp: test a mature business entering a new domain
target network: Nevada w/ 11.5K users; 2.1K items
source network: Arizona w/ 19.5K users; 6.3K items
overlapping: 4.3K users; no items

Epinions: test an emerging business partially aligned with a developed business



WNMF + geometric regularization

- WNMF: weighted nonnegative matrix factorization
- Hete-MF: WNMF+ PathSim between items only
- Hete-CF: WNMF + PathSim between users/items
- Hete-PRW: WNMF + Pairwise RW similarity between users/items
- Amp-MF: WNMF + AmpSim between users/items

Transfer learning based methods

- CMF: collective matrix factorization w/ alignment regularization
- RMGM: rating-matrix generative model
- Amp-CMF: proposed method

cold-start: test on users who have ≤ 5 ratings in training set
90% (55%) of users are cold-start users in Yelp (Epinions)

Yelp (Overall)

Method	RMSE		MAE		RMSE		MAE	
	k=10	k=20	k=10	k=20	k=10	k=20	k=10	k=20
WNMF	1.446 ± 0.009	1.429 ± 0.009	1.097 ± 0.006	1.083 ± 0.005	1.535 ± 0.014	1.520 ± 0.013	1.184 ± 0.005	1.170 ± 0.005
Hete-MF	1.429 ± 0.009	1.351 ± 0.009	1.086 ± 0.005	1.006 ± 0.005	1.518 ± 0.012	1.492 ± 0.011	1.171 ± 0.005	1.148 ± 0.005
Hete-CF	1.305 ± 0.008	1.199 ± 0.008	0.957 ± 0.005	0.907 ± 0.005	1.378 ± 0.009	1.228 ± 0.009	1.017 ± 0.005	0.935 ± 0.005
Hete-PRW	1.343 ± 0.008	1.313 ± 0.008	1.018 ± 0.005	0.991 ± 0.005	1.414 ± 0.008	1.382 ± 0.008	1.088 ± 0.005	1.059 ± 0.005
Amp-MF	1.191 ± 0.009	1.187 ± 0.009	0.899 ± 0.005	0.897 ± 0.005	1.219 ± 0.008	1.215 ± 0.008	0.928 ± 0.005	0.925 ± 0.005
CMF	1.294 ± 0.009	1.274 ± 0.010	0.966 ± 0.005	0.949 ± 0.006	1.349 ± 0.012	1.329 ± 0.012	1.015 ± 0.005	0.998 ± 0.006
RMGM	1.240 ± 0.009	1.238 ± 0.009	0.925 ± 0.005	0.902 ± 0.004	1.316 ± 0.009	1.295 ± 0.009	0.995 ± 0.004	0.974 ± 0.004
Amp-CMF	1.134 ± 0.009	1.127 ± 0.009	0.854 ± 0.005	0.847 ± 0.005	1.148 ± 0.009	1.139 ± 0.009	0.875 ± 0.006	0.865 ± 0.006

Yelp (Cold Start)

Epinions (Overall)

Method	RMSE		MAE		RMSE		MAE	
	k=10	k=20	k=10	k=20	k=10	k=20	k=10	k=20
WNMF	1.551 ± 0.009	1.533 ± 0.009	1.156 ± 0.008	1.153 ± 0.009	1.596 ± 0.016	1.594 ± 0.016	1.219 ± 0.016	1.218 ± 0.013
Hete-MF	1.402 ± 0.010	1.398 ± 0.009	1.034 ± 0.009	1.030 ± 0.008	1.462 ± 0.017	1.454 ± 0.014	1.106 ± 0.016	1.101 ± 0.013
Hete-CF	1.148 ± 0.008	1.141 ± 0.008	0.908 ± 0.007	0.901 ± 0.007	1.211 ± 0.011	1.201 ± 0.011	0.961 ± 0.009	0.955 ± 0.009
Hete-PRW	1.395 ± 0.009	1.392 ± 0.009	1.039 ± 0.005	1.030 ± 0.005	1.434 ± 0.009	1.428 ± 0.009	1.072 ± 0.005	1.066 ± 0.005
Amp-MF	1.099 ± 0.009	1.097 ± 0.009	0.869 ± 0.005	0.868 ± 0.005	1.131 ± 0.009	1.128 ± 0.009	0.899 ± 0.005	0.897 ± 0.005
CMF	1.152 ± 0.007	1.143 ± 0.007	0.870 ± 0.004	0.868 ± 0.005	1.198 ± 0.012	1.185 ± 0.010	0.902 ± 0.009	0.899 ± 0.009
RMGM	1.246 ± 0.008	1.242 ± 0.010	0.989 ± 0.005	0.983 ± 0.007	1.271 ± 0.005	1.266 ± 0.009	1.013 ± 0.002	1.014 ± 0.006
Amp-CMF	1.097 ± 0.009	1.095 ± 0.009	0.867 ± 0.005	0.866 ± 0.005	1.129 ± 0.009	1.127 ± 0.009	0.898 ± 0.005	0.896 ± 0.005

Epinions (Cold Start)

Conclusion:

1. Methods using more accurate similarity measure achieve better performance
2. Combining both geometric and alignment regularization boosts the performance
3. Learning from highly overlapped networks can achieve better improvement: improve 21% in Yelp and 29% in Epinions

5. Acknowledgments

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